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Magneto-optical spectra of closely spaced magnetite nanoparticles

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The Faraday rotation spectrum of composites containing magnetite nanoparticles is found to be dependent on the interparticle spacing of the constituent nanoparticles. The composite materials are prepared by combining chemically synthesized Fe$_3$O$_4$ (magnetite) nanoparticles (8-nm diameter) and poly(methylmethacrylate). Composites are made containing a range of nanoparticle concentrations. The peak of the main spectral feature depends on nanoparticle concentration; this peak is observed to shift from approximately 470 nm for (dilute composites) to 540 nm (concentrated). We present a theory based on the discrete-dipole approximation which accounts for optical coupling between magnetite particles. Qualitative correlations between theoretical calculations and experimental data suggest that the shifts in spectral peak position depend on both interparticle distance and geometrical configuration. © 2005 American Institute of Physics.

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INTRODUCTION

The coupling of light with structures much smaller than the light’s wavelength (typically, interaction lengths less than 100 nm) is particularly relevant with the current push to fabricate photonic devices on the nanometer scale. Previous studies of these optical near-field interactions have focused mostly on noble-metal nanoparticles which display resonances in the optical-absorption spectrum dependent on the particle size, shape, and interparticle spacing. In addition, light has been shown to propagate along noble-metal nanoparticle chains. Here, we extend the investigations of near-field optical interactions and include a study of the magneto-optical properties of nanoparticles as a function of interparticle spacing. Magneto-optically active nanoparticles could have applications in the emerging field of nanophotonics, data storage, or sensing.

The magneto-optical properties of films containing dilute concentrations of Fe$_3$O$_4$ (magnetite) particles have previously been studied. In fact, we recently reported that shifts in the Faraday rotation spectrum of magnetite/polymer nanocomposites are observed with changes in the nanoparticle size, with particle diameters ranging from 8 to 200 nm. In this paper, we report on shifts in Faraday rotation peak position dependent on the concentration of nanoparticles in the matrix. We estimate that the magnetite particles are separated (on average) by distances as small as a few nanometers. To explain these results, we present a new theory based on the discrete-dipole approximation which accounts for optical dipole-dipole coupling between the magnetite particles. Although our model is currently limited to two interacting spheres, we can gain a qualitative understanding of the origin of the spectral shifts.

THEORY

The nanocomposite materials are modeled using a modification of the discrete-dipole approximation (DDA). In our calculation, each particle is approximated by a dipole located at the point $\mathbf{r}_j$ with polarizability tensor $\mathbf{a}_j$. The polarization of the dipole is given by $\mathbf{P}_j=\mathbf{a}_j \mathbf{E}_j$, where $\mathbf{E}_j$ is the local electric field at point $\mathbf{r}_j$. When exposed to light, this electric field is the sum of the incident field and the field emitted by all neighboring dipoles:

$$\mathbf{E}_{\text{dipole},j} = - \sum_{k \neq j} \mathbf{A}_{jk} \mathbf{P}_k,$$

where

$$\mathbf{A}_{jk} = \frac{e^{ikr_{jk}}}{r_{jk}} \left[ \kappa^2 \left( r_{jk} \hat{r}_{jk} - 1 \right) + \frac{ikr_{jk}}{r_{jk}^2} \left( 3r_{jk} \hat{r}_{jk} - \hat{1} \right) \right],$$

and $r_{jk}$ is the distance from particle $j$ to particle $k$ and $\hat{r}_{jk}$ is the unit vector in the $r_{jk}$ direction with $\kappa=\omega \mu / c$. The $3 \times 3$ identity matrix is represented by $\hat{1}$. For $N$ particles, the polarizations, of each particle $\mathbf{P}_j$ can then be determined by solving the system of $3N$ complex linear equations

$$\sum_{k=1}^N \mathbf{A}_{jk} \mathbf{P}_k = \mathbf{E}_{\text{inc},j},$$

where

$$\mathbf{A}_{jj}^{-1}.$$
In order to adapt the DDA method to magneto-optical materials, we transform the dielectric tensor to the right-left (rl) circularly polarized coordinate system with the usual transformation

\[
\bar{\varepsilon} = \begin{pmatrix}
\varepsilon_{xx} & i\varepsilon_{xy} & 0 \\
-i\varepsilon_{xy} & \varepsilon_{xx} & 0 \\
0 & 0 & \varepsilon_{xx}
\end{pmatrix}.
\]

(5)

where

\[
\bar{\varepsilon} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 & 0 \\ -i & i & 0 \\ 0 & 0 & \sqrt{2} \end{pmatrix}.
\]

(7)

This allows us to use the Clausius–Mossotti principle to find the polarizability of the sphere in this coordinate system\textsuperscript{11}

\[
\alpha_{j,u}^{rl} = a^3 \frac{\varepsilon_{j,u}^{rl} - \varepsilon_{hst}}{\varepsilon_{j,u}^{rl} + 2\varepsilon_{hst}},
\]

(8)

where \(a\) is the radius of the spherical particle, \(u\) is the diagonalized component (right, left, and \(z\)), and \(\varepsilon_{hst}\) is the dielectric constant of the host medium. Transforming the matrix \(\tilde{A}_{jk}\) and the vectors \(\tilde{P}_k\) and \(\tilde{E}_{inc,j}\) into the circular coordinate system with Eq. (7) yields

\[
\sum_{k=1}^{N} \tilde{A}_{jk}^{rl} \tilde{P}_k^{rl} = \tilde{E}_{inc,j}^{rl},
\]

(9)

with \(\tilde{A}_{jj}^{rl} (\bar{\varepsilon}^{rl})^{-1}\). Solving Eq. (9) for the polarizations \(\tilde{P}_k^{rl}\), an effective polarizability is determined from a volume average of the calculated polarizations. The Faraday rotation spectra\textsuperscript{12} were calculated from the average dielectric components which were found by using the inverse of the Clausius-Mossotti relation and the averaged polarizability.

In our calculations, we used literature values for diagonal components of the dielectric tensor of \(\text{Fe}_3\text{O}_4\) in Eq. (5) taken from the data reported by Schlegl et al.\textsuperscript{13} and off-diagonal components taken from Zhang et al.\textsuperscript{14} A dielectric constant of 2.25 was used for the poly (methylmethacrylate) (PMMA) (\(\varepsilon_{hst}\)).

\section*{EXPERIMENT}

Magnetite nanoparticles were synthesized using the method of Caruntu et al.\textsuperscript{15} Briefly, \(\text{FeCl}_3\) and \(\text{FeCl}_2\) were dissolved in diethylene glycol yielding a solution containing \(\text{Fe}^{3+}\) and \(\text{Fe}^{2+}\) ions in the ratio of 2:1. Coprecipitation with NaOH at \(\sim 200\) °C resulted in 8–10-nm \(\text{Fe}_3\text{O}_4\) particles. The nanoparticles were washed, dried, and suspended in toluene by the addition of oleic acid as a capping ligand. The concentration of this solution was approximately 5 mg/ml. Varying amounts of this nanoparticle solution were then mixed with a 10% solution of PMMA and toluene. Thin films were prepared by spin coating 20 µl of the solution onto quartz disks for 9 min at 150 rpm. Spectral Faraday rotation measurements were made in the polar configuration using the photoelastic modulator technique\textsuperscript{16} as described in Ref. 6.

\section*{RESULTS AND DISCUSSION}

Figure 1 shows the Faraday rotation spectra of magnetite nanoparticle/PMMA composite films. By increasing the concentration of magnetite in the composite materials, shifts in the main spectral feature of the Faraday rotations by up to approximately 70 nm are observed. Films produced with dilute concentrations exhibited peaks at approximately 470 nm, while those at higher concentrations shifted towards red wavelengths. The largest shift was observed for the most concentrated composite at approximately 540 nm.

These shifts in the spectral peak are not predicted by effective-medium theory (EMT) which does not account for optical interactions between the particles.\textsuperscript{12} We use our modified DDA model to explicitly account for particle-particle interactions. Here, we limit the calculations to two coupled \(\text{Fe}_3\text{O}_4\) nanoparticles and find that this is sufficient to reproduce the qualitative features of the measured Faraday rotation spectrum. We calculate the spectrum for the three basic two-particle geometries shown in Figs. 2–4. In these calculations, the magnetic field is parallel to the direction of light propagation, taken to be the \(z\) direction, consistent with Eq. (5) and the polarization of the incident light is in the \(x\) direction.

For all particle geometries, little change was seen in the spectra until the particles were brought within approximately 7 or 8 nm of each other. In fact, for interparticle distances greater than 8 nm, our calculation is similar to EMT, which is included in the figures for comparison. Figure 2 shows the theoretical results for two particles aligned on the \(x\) axis perpendicular to the propagation direction and parallel to the linear polarized light. This geometry shows a progressive redshift to approximately 500 nm for dipoles with a 3-nm spacing. In Fig. 3, the particles are, again, aligned perpendicular to the propagation direction but with the incident light polarized perpendicular to the particles. Redshifts are shown with a maximum at around 510 nm, but little differ-
figure 2: Calculation of the spectral Faraday rotation for two closely spaced 8-nm Fe$_3$O$_4$ spheres. The direction of the propagation and the polarization of the optical field are indicated in the inset. The EMT calculation (solid line) overlaps completely with the modified DDA calculation for 100-nm dipole separation (solid squares).

figure 3: Calculation of the spectral Faraday rotation for the polarization direction perpendicular to the two-sphere axis.

figure 4: Calculation of the spectral Faraday rotation for light propagating along the axis of the two-sphere system.

The optical coupling is due to near-field interactions, the polarizability of a nanoparticle is determined by the contributions of its nearest neighbors.

**CONCLUSION**

Peak position of the Faraday rotation spectrum of magnetite/PMMA nanocomposite films is shown to be concentration dependent. By increasing the concentration of 8-nm particles in the PMMA matrix, a redshift and broadening of the main spectral feature are observed. Calculations using existing EMT models fail to account for the shifts seen in the experimental data. Using a DDA-based model, the shifts in peak position are shown to occur based purely on optical effects where only the interparticle distance is varied. In addition, the peak positions of the calculated spectra depend on the geometrical configuration. In future work, we will extend our calculations to include clusters of randomly distributed particles to explain more quantitatively our experimental data.

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