Automating Lackenby's Method: The Design of a Set of Scripts to Execute Lackenby's Method with McNaull's Expansion in Rhinoceros 3D

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Automating Lackenby’s Method: The Design of a Set of Scripts to Execute Lackenby’s Method with McNaul’s Expansion in Rhinoceros 3D

A Thesis

Submitted to the Graduate Faculty of the University of New Orleans in partial fulfillment of the requirements for the degree of

Master of Science in Engineering in Engineering Naval Architecture and Marine Engineering

by

Mara Kramer

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Abstract

In vessel design, modifying the design of a preexisting hull is a common practice to save time and labor compared to designing a hull from scratch. This can be achieved either by manually adjusting the hull model in a 3D modeling software or by systematically adjusting certain vessel parameters using an algebraic method. However, these methods are time-intensive and do not fully utilize the capabilities of modern software. To address this issue, this paper presents a set of Rhinoscript and Python scripts that automate part of the hull modification process using Lackenby’s method with McNaull’s expansion. The developed code utilizes provided hull offsets (comma-separated values, CSV, file), along with user-input values, to perform the desired Lackenby shift. The resulting modified hull surface is displayed in Rhino alongside the original hull surface. The developed scripts demonstrate the potential of modern software to enhance the efficiency and accuracy of vessel design.

Keywords: hull design, Lackenby, McNaull, Python, Rhino, Rhinoscript
1. Introduction

When designing vessels, modifying existing hull designs to meet current project specifications is a common tactic for saving labor time and expense. However, many firms do not take advantage of the capabilities of modern 3D modeling software. Rhinoceros 3D (Rhino) is a popular software among naval architecture firms, with its own coding language, Rhinoscript, built off the Python language. While Rhinoscript is admittedly still rather restricted, it can be used to semi-automate many design processes where a 2D or 3D object is a desired outcome. This project leverages Rhinoscript to create a set of scripts for modeling a derived hull from a parent hull using Lackenby’s method with McNaul’s expansion.

This paper presents a breakdown of the operation of each script written, as well as the theory and methodology for the hull modification methods used within. The main script, written in Rhinoscript, performs various functions to maximize the program’s potential functionality, with a focus on reducing user interaction. The script can modify a monohull vessel using user input values and a comma-separated values (CSV) file containing station offsets, returning 3D surface models of both the parent and derived hull, as well as data files.

Section 2 delves into the theory behind Lackenby’s method, McNaul’s modifications, and Akima interpolation – the fundamental theoretical components for this project. Section 3 provides an overview of each script developed to execute the Lackenby shift in Rhino, discussing their format and functionality. Section 4 showcases a sample vessel used to demonstrate the code’s functionality, while Section 5 presents and evaluates the results obtained from the sample vessel. Finally, Section 6 summarizes the conclusions drawn from this project, discusses future work, and examines potential applications.
2. Theory

Over the years, many methods have been developed to help optimize the hull design process. One such method, commonly employed in the 1900s, used series of parent hulls as templates for newly developed hulls. These series documented the best combinations of geometric variations in length, beam, and depth that resulted in the least amount of resistance for various vessel forms (planing vessel, tanker, etc.) and were early attempts of systematic variation. Examples of standard series include: Taylor series, Series 60, Swedish tanker and cargo series, German HSVA series, and the British BSRA series (Taylor). Interestingly, some standard series (i.e. the British BSRA series) used Lackenby’s method in development. However, limitations of this method have become progressively more apparent as vessel designs become increasingly complex and optimized, particularly in military applications, where the design of vessels is critical for gaining an edge over potential adversaries.

As a result, new methods (particularly lines distortion and parametric hull generation) have received increased attention. The dominant methods of lines distortion are Lackenby’s method (Lackenby) and McNaull’s modification and expansion of Lackenby’s method (McNaull). Two notable examples of parametric hull design methods are the “Parametric Generation of Yacht Hulls” (Bole) and “Parametric Design and Hydrodynamic Optimization of Ship Hull Forms” (Harries). Bole’s report identified factors and parameters critical in yacht design and investigated several parametric methods to generate a yacht hull form. The parametric methods developed use a combination of B-splines and defined parameters in order to complete the calculations. While this method offers a comparative alternative to a lines distortion approach, it is limited in application to yacht design (Bole).
Harries investigates the use of Lackenby’s method for 3D hull modeling and develops a comprehensive parametric design method intended for use with 3D modeling software and computer programs. Regarding Lackenby’s method for hull design, Harries concludes that “the approach is not flexible enough to control the design in detail” and that the method with which Lackenby’s method is executed is “too inflexible for hydrodynamic improvement in real fluid”. Harries’s parametric method is particularly suited for 3D software or automation due to its accuracy in meeting desired properties and ability to maintain fairness of a hull form (Harries). Theoretically, this parametric method does not have any disadvantages; however, it is not suitable for use in this project for several reasons:

- This method generates a hull form from scratch rather than using a parent hull form
- Executing this method is computationally intensive and time-consuming
- The current scripting tools available in Rhino are limited and would not be able to perform the computations required to complete the parametric design method

Therefore, despite its flaws, Lackenby’s method with McNaull’s expansion was chosen for this project due to its simplicity and suitable accuracy for preliminary hull design.

2.1. Lackenby’s Method

In Lackenby’s 1950 paper “On the Systematic Geometrical Variation of Ship Forms”, equations for the independent variation of three separate parameters – prismatic coefficient ($C_p$), longitudinal center of buoyancy (LCB), and extent of the parallel midbody ($p$) – by distorting the sectional area curves of a parent vessel were derived. Lackenby’s method was a significant advancement compared to traditional techniques, such as “swinging” the sectional area curve to shift the longitudinal center of buoyancy, which lacked control over the position of the parallel midbody or the position of the maximum section. McNaull emphasized the importance of
Lackenby’s method, stating that it “represented a significant improvement over such traditional methods” (McNaul).

The first method (“one minus prismatic” variation) presented in Lackenby’s paper splits the vessel into fore- and aft-bodies at midship so that both ends of the vessel are varied independently. The term “one minus prismatic” is drawn from the equations derived that share the term \((1 - \phi)\), where \(\phi\) is the prismatic coefficient of the half-body. Each half-body uses the same set of variables as shown in the table and figure below, with subscript \(A\) denoting the aftbody and \(F\) indicating a parameter of the forebody. However, this linear shift method does not allow for the independent variation of the parallel midbody. An in-depth discussion of equations will be saved for Section 2.2 when discussing McNaul’s modifications.

Table 1: Half-body variables for “one-minus prismatic” variation (Lackenby).

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\bar{x})</td>
<td>The fractional distance from midship of the centroid of the half-body</td>
</tr>
<tr>
<td>(p)</td>
<td>The fractional parallel middle of the half-body</td>
</tr>
<tr>
<td>(x)</td>
<td>The fractional distance of any transverse section from midship</td>
</tr>
<tr>
<td>(y)</td>
<td>The area of the transverse section at (x) expressed as a fraction of the maximum ordinate</td>
</tr>
<tr>
<td>(\delta \phi)</td>
<td>The required change in prismatic coefficient of the half-body</td>
</tr>
<tr>
<td>(\delta p)</td>
<td>The consequent change in parallel middle body</td>
</tr>
<tr>
<td>(\delta x)</td>
<td>The necessary longitudinal shift of the section at (x) to produce the required change in prismatic coefficient</td>
</tr>
<tr>
<td>(h)</td>
<td>The fractional distance from midship of the centroid of the added “sliver” of area represented by (\delta \phi)</td>
</tr>
</tbody>
</table>
Figure 1: “One minus prismatic” linear variation of a half-body (Lackenby).

Since the parallel midbody shift cannot be controlled with the above method, Lackenby developed a second method employing a quadratic shift. This method allows for the independent variation of the parallel midbody (in addition to the LCB and prismatic coefficient) by considering the radius of gyration \( k \) as a variable. The variables used in this diagram have the same significance as defined for the “one minus prismatic” variation method (Lackenby).
Although the quadratic sectional area curve variation method Lackenby developed was a significant improvement over traditional methods, it has some limitations. Lackenby assumed that the boundary between the forebody and aftbody was located at the midship station and neglected any stations forward of the forward perpendicular. This assumption means that the length of the fore- and aft-bodies are equal, which is incredibly difficult to work with considering the complexity of contemporary vessels. Contemporary vessels often have complex, significant appendages such as bulbous bows that have non-negligible volumes. Moreover, Lackenby’s system of equations was solved using successive (back) substitution. This iterative method assumes that values will converge quickly, making it suboptimal for quick modifications or design. Therefore, there was a need to develop a more comprehensive lines distortion method (McNaull).

### 2.2. McNaull’s Modifications

In the 1980 paper by McNaull, a modified and extended version of Lackenby’s method is presented, which overcomes the limitations of the original work. McNaull introduces two sets of
linear simultaneous equations, where the first corrects Lackenby’s limitations and arranges the equations in a matrix form to make them easier and faster to solve. The second set expands Lackenby’s method from 10 simultaneous equations to 12 to allow for the independent variation of prismatic coefficient, LCB, parallel midbody, and slope of the entrance or run. The addition of the variables for entrance/run slope changes the equations for longitudinal station shift to cubic compared to the original quadratic form. McNaull presents a similar diagram to those provided by Lackenby, but with his addition of slope variables.

Figure 3: Cubic variation of a half-body (forebody) (McNaull).

McNaull defines his variables in the above figure with reference to the forebody. Aftbody variables are analogous to the following definitions using the subscript $A$. 

![Diagram](image-url)
Table 2: Half-body variables for cubic variation (McNaull).

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V_F$</td>
<td>(parent) underwater volume of forebody</td>
</tr>
<tr>
<td>$x_F$</td>
<td>(parent) x-value of the centroid of $\nabla F$</td>
</tr>
<tr>
<td>$p_F$</td>
<td>(parent) length of the parallel midbody</td>
</tr>
<tr>
<td>$L_F$</td>
<td>(parent) length of the forebody</td>
</tr>
<tr>
<td>$A_M$</td>
<td>(parent) maximum sectional area</td>
</tr>
<tr>
<td>$x$</td>
<td>(parent) x-value of a point on the forebody sectional area curve</td>
</tr>
<tr>
<td>$A_S(x)$</td>
<td>(parent) sectional area corresponding to $x$</td>
</tr>
<tr>
<td>$\theta_{PF}$</td>
<td>(parent) slope of the entrance of the forebody</td>
</tr>
<tr>
<td>$\delta V_F$</td>
<td>(derived) change in volume</td>
</tr>
<tr>
<td>$x_{\delta F}$</td>
<td>(derived) x-value of the centroid of $\delta V_F$</td>
</tr>
<tr>
<td>$\delta p_F$</td>
<td>(derived) change in parallel midbody</td>
</tr>
<tr>
<td>$\delta x$</td>
<td>(derived) longitudinal shift of station at $x$</td>
</tr>
<tr>
<td>$\theta_{DF}$</td>
<td>(derived) slope of the entrance of the forebody</td>
</tr>
</tbody>
</table>

McNaull’s modification of Lackenby’s original equations for a station shift results in the following quadratic equation for a half-body (forebody)

$$\delta x = Ax^2 + Bx + C$$  \hspace{1cm} \text{Equation 1}$$

where $A$, $B$, and $C$ are constants derived from four boundary conditions

$$\delta x = \delta p_F = Ap_F^2 + Bp_F + C \hspace{0.5cm} \text{at} \hspace{0.5cm} x = p_F, \hspace{0.5cm} \delta x = \delta p_F$$ \hspace{1cm} \text{Equation 2}$$

$$\delta x = 0 = AL_F^2 + BL_F + C \hspace{0.5cm} \text{at} \hspace{0.5cm} x = L_F, \hspace{0.5cm} \delta x = 0$$ \hspace{1cm} \text{Equation 3}$$

$$\delta V_F = 2A \nabla F x_F + B \nabla F + CA_M \hspace{0.5cm} \text{where} \hspace{0.5cm} \delta \nabla F = \int_0^{A_M} \delta x \, dA_S$$ \hspace{1cm} \text{Equation 4}$$

$$x_{\delta F} \delta V_F = 3A \nabla F k_F^2 + 2B \nabla F x_F + C \nabla F \hspace{0.5cm} \text{where} \hspace{0.5cm} x_{\delta F} \delta \nabla F = \int_0^{A_M} x \, \delta x \, dA_S$$ \hspace{1cm} \text{Equation 5}$$

where $k_F$ is the radius of gyration about midship. With this set of equations for the forebody, there are five unknown values: $A$, $B$, $C$, $\delta V_F$, and $x_{\delta F}$. The aftbody uses the unknowns $D$, $E$, $F$, $\delta V_A$. 

8
and $\chi_{\delta A}$. Therefore, combining the equations for the fore- and aft- bodies, a matrix of 10 simultaneous equations for a parabolic longitudinal shift of a vessel’s stations is developed.

$$
\begin{bmatrix}
\delta p_F \\
0 \\
0 \\
0 \\
\delta p_A \\
0 \\
0 \\
0 \\
\delta \nabla \\
(\nabla + \delta \nabla)(x_{LCB} + \delta x_{LCB}) - \nabla x_{LCB}
\end{bmatrix}
= 
\begin{bmatrix}
A \\
B \\
C \\
\delta \nabla_F \\
x_{\delta F} \delta \nabla_F \\
D \\
E \\
F \\
\delta \nabla_A \\
x_{\delta A} \delta \nabla_A
\end{bmatrix}
$$

Equation 6

When considering the slope of the entrance and run of the vessel, the matrix gains two unknown variables, therefore increasing the equations for longitudinal shifts from quadratic to cubic and the resulting matrix from 10 simultaneous equations to 12. However, an analogous derivation process is followed.

$$
\delta x = Ax^3 + Bx^2 + Cx + D
$$

Equation 7

$$
\tan \theta_{PF} \cot \theta_{DF} - 1 = 3AL_F^2 + 2BL_F + C \quad \text{at } x = L_F, \frac{dy}{dx} = \text{spec. value}
$$

Equation 8

$$
\delta x = \delta p_F = Ap_F^3 + Bp_F^2 + Cp_F + D \quad \text{at } x = p_F, \delta x = \delta p_F
$$

Equation 9
\[
\delta x = 0 = AL_F^3 + BL_F^2 + CL_F + D \quad \text{at } x = L_F, \delta x = 0 \quad \text{Equation 10}
\]

\[
\delta \nabla_F = 3A\nabla_F k_F^2 + 2B\nabla_F x_F + C\nabla_F + DA_M \quad \text{where } \delta \nabla_F = \int_0^{A_M} \delta x \, dA_S \quad \text{Equation 11}
\]

\[
x_{\delta F}\delta \nabla_F = 4A\nabla_F R_F^3 + 3B\nabla_F k_F^2 + 2C\nabla_F x_F + D\nabla_F \quad \text{where } x_{\delta F}\delta \nabla_F = \int_0^{A_M} x \, \delta x \, dA_S \quad \text{Equation 12}
\]

where \( \tan \theta_{PF} \) is the slope of the parent curve, \( \cot \theta_{DF} \) is the inverse of the slope of the derived curve, and \( R_F \) is the lever of the third moment of volume about midship. Each half-body has six unknowns with A, B, C, D, \( \delta \nabla_F \), and \( x_{\delta F} \) referring to the forebody and E, F, G, H, \( \delta \nabla_A \), and \( x_{\delta A} \) referring to the aftbody (McNaul).
\[
\begin{bmatrix}
\tan \theta_{PF} \cot \theta_{DF} - 1 \\
\delta p_F \\
0 \\
0 \\
0 \\
\tan \theta_{PA} \cot \theta_{DA} - 1 \\
\delta p_A \\
0 \\
0 \\
\delta \nabla \\
(\nabla + \delta \nabla)(x_{LCB} + \delta x_{LCB}) - \nabla x_{LCB}
\end{bmatrix}
= \\
\begin{bmatrix}
3L_F^2 & 2L_F & 1 \\
p_F^3 & p_F^2 & p_F & 1 \\
L_F^3 & L_F^2 & L_F & 1 \\
3\nabla_F k_F^2 & 2\nabla_F x_F & \nabla_F & A_{MF} & -1 \\
4\nabla_F R_F^2 & 3\nabla_F k_F^2 & 2\nabla_F x_F & \nabla_F & 0 & -1 \\
1 & 1
\end{bmatrix}
\begin{bmatrix}
A \\
B \\
C \\
D \\
\delta \nabla_F \\
x_{DF} \delta \nabla_F \\
E \\
F \\
G \\
H \\
\delta \nabla_A \\
x_{DA} \delta \nabla_A
\end{bmatrix}
\]

Equation 13

These matrices can be easily solved using a Gaussian elimination process. It was deemed appropriate to use the expanded matrix (Equation 13) for this project, as there is no reason not to use it over the quadratic matrix.

2.3. Higher Order Moment Derivations

An alternative method is necessary to calculate the areas, moments, and volumes required for the cubic longitudinal shifts since Rhinoscript does not allow use of Python libraries dedicated to complex math, interpolation, or statistics. Dr. Lothar Birk’s paper “A Comprehensive and
Practical Guide to the Hess and Smith Constant Source and Dipole Panel” lays the groundwork for an algebraic method to calculate moments and areas with a quadrilateral panel method. The method used in this paper is based on Stokes theorem and can be applied to any planar polygon.

Figure 4: Discretization of a ship bow into quadrilateral and triangular panels (Birk).

This method defines four temporary panel corners for a discretized location on the surface of the hull and the area and centroid of the quadrilateral are found using an algebraic sum method. Starting with following surface integral

\[
\iint_S \left( \frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dxdy = \oint_C P \, dx + \oint_C Q \, dy
\]

Equation 14

the functions \( P \equiv 0 \) and \( Q \equiv x \) will result in the following equation for area (which has been generalized for a planar polygon with \( n \) number of vertices).

\[
A = \oint_C x \, dy = \sum_{i=0}^{n} \int_{y_i}^{y_{i+1}} x \, dy
\]

Equation 15

Since the polygon sides are assumed to be straight, the parametric forms of \( x \) and \( y \) can be used

\[
x = (x_{i+1} - x_i) t + x_i
\]
\[ y = (y_{i+1} - y_i)t + y_i \]

the area equation can be simplified to the following algebraic form

\[ A = \frac{1}{2} \sum_{i=0}^{n} (y_{i+1} - y_i)(x_i - x_{i+1}) \]

Equation 16

Within the script, the area equation was also used to calculate volume by swapping out the individual points within a cross-section for the arrays of cross-sections and x-locations of the stations. To derive the y-moment, the power of Q is raised to \( Q \equiv \frac{x^2}{2} \) and P remains at zero.

\[ M_y = \frac{1}{6} \sum_{i=0}^{n} (y_{i+1} - y_i)(x_i^2 + x_i x_{i+1} + x_{i+1}^2) \]

Equation 17

Analogously, setting Q to zero and \( P \equiv -\frac{y^2}{2} \) will result in an equation for x-moment (Birk).

\[ M_x = -\frac{1}{6} \sum_{i=0}^{n} (y_i^2 + y_i y_{i+1} + y_{i+1}^2)(x_{i+1} - x_i) \]

Equation 18

For the Lackenby shift, the second order moment of volume and third order moment of volume are needed, both of which can be derived in similar fashion to the y-moment. The second order moment of volume sets \( Q \equiv \frac{x^3}{3} \) with \( P \equiv 0 \) and the third order moment of volume defines \( Q \equiv \frac{x^4}{4} \) and \( P \equiv 0 \).

\[ I = \frac{1}{12} \sum_{i=0}^{n} (y_{i+1} - y_i)(x_{i+1}^3 + x_{i+1}^2 x_i + x_{i+1} x_i^2 + x_i^3) \]

Equation 19

\[ J = \frac{1}{20} \sum_{i=0}^{n} (y_{i+1} - y_i)(x_{i+1}^4 + x_{i+1}^3 x_i + x_{i+1}^2 x_i^2 + x_{i+1} x_i^3 + x_i^4) \]

Equation 20

### 2.4. Akima Interpolation

The Akima interpolation method is commonly used for various applications, including in Python libraries containing interpolation functions. In this project, it is utilized to discretize the station data points, allowing the areas to become accurate closed panel-defined objects suitable for
panel-method integration. Akima interpolation also fits a smooth curve to a set of data points, making it an appropriate interpolation method for a ship hull as it retains maximum curve definition when creating a panel-defined shape from the original curve offsets. Interpolated curve points are temporarily added to the set of station offsets to produce a panel object with higher fidelity. Since access to standard Python libraries was not available, the Akima interpolation method was implemented in an auxiliary file, akimaint.py. Additional information on Akima interpolation and the auxiliary script is available in the supplementary paper introduced in Appendix A (Akima).
3. Code Overview

In Rhinoscript, the commonly available extension modules such as “numpy” or “scipy” (used for math, integration, interpolation, etc.) are not available. Hence, auxiliary scripts were written in Python that can replicate the capabilities required to complete Lackenby’s method. The auxiliary scripts are as follows:

- akimaint.py: contains the functions for Akima interpolation
- cubicmatrix.py: defines the $12 \times 12$ matrix
- gauss.py: contains a simple Gaussian elimination algorithm to solve the matrix
- offsetimport.py: defines a function to import station data from a CSV file and convert the data into coordinate points separated by station
- secarea.py: script containing functions for calculating sectional area, area moments, second order moment of volume, and third order moment of volume

Sections 3.1 and 3.2 discuss the theory behind cubicmatrix.py and secarea.py, respectively. Section 3.3 discusses the structure and components of the main script, main.py. For a comprehensive discussion of the auxiliary scripts and the user interface (UI) developed for the main script, please refer to Appendix A.

3.1. McNaull Cubic Matrix (cubicmatrix.py)

The role of cubicmatrix.py is to define the $12 \times 12$ matrix derived in McNaull’s expansion of Lackenby’s method. However, instead of using the inverses of the slopes of the derived curve at fore and aft, $\cot \theta_{DF}$ and $\cot \theta_{DA}$, the script uses the inverses of the slopes of the parent curve, $\cot \theta_{PF}$ and $\cot \theta_{PA}$, assuming that the slopes of the parent and derived curves are equal. This decision was made to simplify the project, as determining the slope of the derived curve with the
limited libraries available would be time-consuming and unnecessary to prove the main script’s functionality.

3.2. **Sectional Area Calculations (secarea.py)**

The secarea.py auxiliary script defines the equations needed to compute the sectional area at each station, as well as equations for both area moments and the higher-order volume moments, based on the derivations presented in Section 2.3. Although the panel method and Akima interpolation could theoretically achieve high accuracy in calculating the sectional area and moments, it is crucial to test the code on a small scale to ensure that the scripts are returning accurate results. Therefore, the defined area and area moment equations were tested within secarea.py using a small CSV file that contains four geometric ship-like sections. First, the test verified that offsetimport.py was correctly importing the station data provided in the CSV file offsets_areatest.csv in Appendix B. Any issues with the code written within offsetimport.py would also show up in this test. Then, the code truncates any points above the defined waterline, uses the Akima interpolation function to calculate additional points for each station to use in the sectional area integration, and appends a corner point to the end of each station array to close the curve in order to apply the integration method derived in Section 2.3. The y-value of the corner point for each station lies on the centerline ($y = 0$), and the z-value is equal to the largest z-value in the modified station array, which equals the defined draft, unless the station is entirely submerged. With the stations fully modified and suitable for panel-method integration, the area and moment equations defined in the script can be used to determine the sectional area, y-center, and z-center of each station.
Figure 5 and Figure 6 below present a comparison between an Excel plot of the station data from the CSV file and the Python generated plot of the sectional areas. The black dashed line on Figure 5 denotes the draft used for testing.

Figure 5: Plot of CSV points used to define the four test stations.

Figure 6: Python generated plot of test sectional areas.
Figure 6 shows that within the testing portion of the script, the stations were successfully truncated at the defined draft and the corner point has been appended on centerline. Additionally, the values within each station are accurate to those shown in Figure 5. Therefore, the first two components of the test script—assessing the proper functionality of offsetimport.py and akimaint.py have been proven. Table 3 below presents a comparison between hand-calculated sectional area values and centroid values for each test station and the results calculated by Python using the functions defined in secarea.py. The only station with any difference within five significant figures is station 3. This station had a trapezoidal underwater area with a sharp angle, as all other stations had a triangular sectional area; therefore, it is not unexpected that a slight deviation might arise when fitting a cubic curve to station 3. The percent differences between the hand-calculated values and script-calculated values within five significant figures for station 3 are 0.029, 0.013, and 0.017 for the sectional area, y-center, and z-center, respectively. Considering the relative insignificance of these differences, the formulas defined within secarea.py are correct, and Akima interpolation is a viable interpolation method for this application.

Table 3: Comparison of hand- and Python-calculated areas and centers.

<table>
<thead>
<tr>
<th>Station</th>
<th>Station x-Position</th>
<th>Calc. Area</th>
<th>Python Area</th>
<th>Calc. Center</th>
<th>Python Center</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.0</td>
<td>2.0000</td>
<td>2.0000</td>
<td>(0.6667,1.3333)</td>
<td>(0.6667,1.3333)</td>
</tr>
<tr>
<td>1</td>
<td>2.0</td>
<td>4.0000</td>
<td>4.0000</td>
<td>(1.3333,1.3333)</td>
<td>(1.3333,1.3333)</td>
</tr>
<tr>
<td>2</td>
<td>3.0</td>
<td>5.5000</td>
<td>5.5016</td>
<td>(1.5606,1.1970)</td>
<td>(1.5608,1.1968)</td>
</tr>
<tr>
<td>3</td>
<td>6.0</td>
<td>1.6000</td>
<td>1.6000</td>
<td>(1.0667,1.6667)</td>
<td>(1.0667,1.6667)</td>
</tr>
</tbody>
</table>
Figure 7 presents a sample sectional area curve created from the four sectional area data points calculated with the test script. The data points are connected with straight lines; Akima interpolation was not used to find a smooth curve fit as Akima interpolation requires at least five data points.

### 3.3. Main Script (main.py)

The main script (Appendix C) uses the functions defined in the auxiliary script in combination with Rhinoscript commands and a UI module to execute the Lackenby shift with minimal user interaction. The automation of the Lackenby shift and ease-of-use were heavily weighted when writing this script as, while a simple scripting of the main script would be functional, it would be incomprehensible to someone unfamiliar with programming. This script should be an accessible quick design tool for all naval architects and designers; therefore, making
the experience as easy and user-friendly as possible was a core consideration. This section overviews the main components of the main script and how it utilizes each auxiliary script.

At the top of the program, a string of text outlines the program description, conditions for usage, credits, and directs users to read the readme.txt file (Appendix E). This file repeats the descriptions and conditions written in the main script and provides instructions for how to run the main script for users unfamiliar with code, Lackenby’s method, or the Rhino software. This script is intended for use with symmetrical, displacement ships, and has only been tested using a monohull hull form. The stations provided in the CSV file should be defined using half-breadths and have a station placed on midship. As no appendages are currently supported, it is assumed that the length between perpendiculars is equal to the length overall. Additionally, the forward perpendicular should have the same x-location as the first station and the aft perpendicular location should coincide with the last station. It is recommended that the CSV file be nondimensionalized with half-breadths defined as a fraction of the maximum half-breadth and elevation points defined as a fraction of the draft/design waterline. However, if the vessel in the CSV file is at full scale, the user can enter a value of 1 for the draft and 2 for the beam within the UI. Scaling the draft by 1 will keep all heights constant, and since the half-breadth needs to remain at a scale of 1 and the beam is twice the width of the half-breadth, the beam will remain true to size if given a value of 2.
The next section imports all the necessary libraries and modules from Rhino, Python, or the auxiliary scripts. “Defining User Interface” defines the classes and functions required to create a UI with the user interface helper classes written by Mark Meier and published to his blog for public use (Meier). The UI classes design a pop-up window that allows the user to enter values necessary to define the vessel, length between perpendiculars (LPP), beam (B), draft (T), and the Lackenby shift variables: change in length of the parallel midship forward of midship (dpf), change in length of the parallel midship aft of midship (dpa), change in prismatic coefficient as a percentage of prismatic coefficient (dCP), and change in LCP as a percentage of LPP (dLCP). All variables are written in a monospaced font as they have been defined within the main program. Further discussion of the UI portion of the main script can be found in Appendix A.

Next, the function (SACfunc) is defined that calculates all the variables necessary to describe the sectional area curve and set the coefficients in McNaul’s 12 × 12 matrix. The inputs for this function are called stations, T, and npts. The array of stations imported from a CSV file using offsetimport.py is stations, T is the user defined draft, and npts is the number of
points used for the Akima interpolation of the stations. SACfunc will output the variables defined below.

Table 4: Definitions of the variables output from SACfunc.

<table>
<thead>
<tr>
<th>Variable Name</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>SAC</td>
<td>Sectional area curve</td>
</tr>
<tr>
<td>xsta</td>
<td>x-position of each station</td>
</tr>
<tr>
<td>AM</td>
<td>Midship area</td>
</tr>
<tr>
<td>V</td>
<td>Volumetric displacement</td>
</tr>
<tr>
<td>CP</td>
<td>Prismatic coefficient</td>
</tr>
<tr>
<td>iSAC</td>
<td>Indices of stations with the maximum sectional area</td>
</tr>
<tr>
<td>iparallelf</td>
<td>Index of the forward extent of the parallel midbody</td>
</tr>
<tr>
<td>iparallela</td>
<td>Index of the aft extent of the parallel midbody</td>
</tr>
<tr>
<td>xm</td>
<td>Position of midship from the forward perpendicular</td>
</tr>
<tr>
<td>Lf</td>
<td>Length of the forebody</td>
</tr>
<tr>
<td>La</td>
<td>Length of the aftbody</td>
</tr>
<tr>
<td>xLCB</td>
<td>Position of the LCB with respect to midship (positive forward)</td>
</tr>
<tr>
<td>CPf</td>
<td>Prismatic coefficient of the forebody</td>
</tr>
<tr>
<td>CPA</td>
<td>Prismatic coefficient of the aftbody</td>
</tr>
<tr>
<td>xLCBf</td>
<td>LCB of the forebody</td>
</tr>
<tr>
<td>xLCBa</td>
<td>LCB of the aftbody</td>
</tr>
<tr>
<td>kf</td>
<td>Radius of gyration of the SAC of the forebody</td>
</tr>
<tr>
<td>ka</td>
<td>Radius of gyration of the SAC of the aftbody</td>
</tr>
<tr>
<td>Rf</td>
<td>Third order moment radius of gyration of the SAC of the forebody</td>
</tr>
<tr>
<td>Ra</td>
<td>Third order moment radius of gyration of the SAC of the aftbody</td>
</tr>
<tr>
<td>thetadf</td>
<td>Slope of the SAC at forward end</td>
</tr>
<tr>
<td>thetada</td>
<td>Slope of the SAC at the aft end</td>
</tr>
</tbody>
</table>

To calculate the above variables, first the sectional area of each station and xsta array are calculated using secarea.py and akimaint.py analogously to the process outlined in Section 3.2. The midship area is found by locating the maximum value within SAC, the volumetric displacement is calculated using the area function in secarea.py with the input variables of xsta and SAC, and the prismatic coefficient follows the formula
\[ C_P = \frac{v}{L_{PP}AM} \]

Then, the variables setting the extent of the fore- and aft-bodies are determined so that the half-bodies can be split for further calculations. The extent of the parallel midbody is found by defining $i_{SAC}$ equal to all station indices that have the maximum cross-sectional area. The indices $i_{parallelf}$ and $i_{parallela}$ are set equal to the first and last indices within the range of $i_{SAC}$, respectively. The position of midship ($x_m$) is set equal to the average of the two indices $i_{parallelf}$ and $i_{parallela}$, unless the vessel has no parallel midship, in which case $i_{parallela}$, $i_{parallelf}$, and $x_m$ are the same. With the midship position defined, the forebody length ($L_f$), aftbody length ($L_a$), and distance between LCB and midship ($x_{LCB}$) can be calculated and ship split into half-bodies.

The process of determining the variables of each half-body is identical for both the forebody and aftbody besides variable names, so it will only be discussed once. First, just as the entire displaced volume was calculated, the volume of the half-body is calculated using the area function using the x-values and the SAC values for the half-body. The prismatic coefficient is calculated analogously. The first order moment, second order moment, and third order moment are calculated using the moment functions defined in secarea.py with the same inputs used when calculating the half-body volume. The LCB of the half-body with respect to midship, radius of gyration of the SAC of the half-body, and third order moment radius of gyration are calculated from the first, second, and third order moments respectively. Finally, the angle of the SAC curve is calculated by taking the inverse tangent of the slope between two points.

With all the necessary variables and functions defined, the code transitions over to execution. First, the UI is called, prompting the user input window to pop up. The values input by the user are then converted to variables to be used within other functions. Next, Rhinoscript
functions and the offsetimport.py script are used to import the ship offsets from a CSV file. These offsets are then unpacked and arranged into an array of stations, a keel line, and a sheer line. With the parent hull in place, the Lackenby shift is now executed by calling the \texttt{SACfunc} function. The absolute change in the prismatic coefficient, volume, and LCB position are calculated from the user input with the following equations:

\begin{align*}
    dxC_p &= dC_p \cdot C_p \quad \text{Equation 22} \\
    dV &= dC_p \cdot A_M \cdot LPP \quad \text{Equation 23} \\
    dxLCB &= dLCB \cdot LPP \quad \text{Equation 24}
\end{align*}

With this, the moment volume of the parent hull required for the cubic matrix is calculated with

\begin{equation}
    MVol = (V + dV) \cdot (xLCB + dxLCB) \quad \text{Equation 25}
\end{equation}

Using the \texttt{Amat} function from cubicmatrix.py and the \texttt{gauss} function from gauss.py, the McNaull’s cubic matrix is formed and solved. The Lackenby shift for each half-body is calculated using Equation 7 and the variables found from the cubic matrix are applied to the stations to get a new set of stations, sheer line, and keel line. With this new set of stations, the last set of calculations is performed: using the \texttt{SACfunc} one more time with the new stations as an input to determine the derived hull data.

Now that both the parent hull and derived hull forms have a complete set of offsets, Rhinoscript commands are used to draw and display the hull forms. First, layers are created to hold the parent and derived hull curves and surfaces using the command \texttt{AddLayer}. For the parent hull, the “Parent Curves” layer is turned on and interpolated curves are created for each set of station offsets using the \texttt{AddInterpCurve} command. Then, the user is prompted to select the parent hull curves, and a network surface is created using \texttt{AddNetworkSurface}. Switching to
the “Parent Hull” layer, the user is prompted to select both the set of curves and the surface, and the hull form is mirrored across centerline with the XformMirror and TransformObjects commands. An analogous process is followed for the derived hull form using the new stations on the “Derived Curves” and “Derived Hull” layers.

The last section of the code writes two data files containing information on the parent and derived hull forms. Much like everything else, the files are analogous to each other, only replacing the variables to reference either the parent or derived hull as appropriate. The unit system used within Rhino is pulled and displayed alongside the user input data entered in the pop-up window. Next the station offsets and sectional area curve data are displayed. Finally, the forebody, aftbody, and other variables calculated within SACfunc are reported.
4. Introduction to the Sample Vessel

A CSV file containing the offsets for an ocean kayak has been designed for the purpose of demonstrating this script (Appendix D). The offsets in the file are defined using stations, half-breadths, and elevations (heights). Additionally, these offsets have been nondimensionalized by scaling the half-breadths as a fraction of the maximum half-breadth and the elevations as a fraction of the design waterline. This format ensures that the kayak can change its size and length/beam ratio easily with user input. The vessel’s body plan, half-breadth plan, sectional area curve, and user input values are shown below. The body plan is split with stations 0-10 on the left side of the centerline, and stations 11-20 on the right.

![Body Plan](image1)

![Half-Breadth Plan](image2)

Figure 9: Parent hull body plan (top) and half-breadth plan (bottom).

The choice to use a kayak model was an error. The author mistakenly assumed that using kayak offsets would be ideal for testing due to the simplistic hull form of a kayak. However, this simplicity proved to be detrimental, as using a parent hull that does not contain a parallel midship restricts the ability to fully test the Lackenby shift. This error will be expanded upon when analyzing the derived hull. Additionally, this model is flawed as it has notable kinks in the waterplane near the bow and aft due to rushed development.
The subpar station design of the vessel is prominent when viewing the sectional area curve of the parent vessel. The first four sectional areas connect in a near parabolic form before abruptly shallowing out to join with the gentler slope of the rest of the forebody run. There is a similar kink at the fourth from last sectional area; however, the change in sectional area slope is less noticeable.

Table 5: Parent hull input values.

<table>
<thead>
<tr>
<th>Input Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>LPP</td>
<td>20.00 ft</td>
</tr>
<tr>
<td>B</td>
<td>3.50 ft</td>
</tr>
<tr>
<td>T</td>
<td>0.50 ft</td>
</tr>
<tr>
<td>dpf</td>
<td>0.00 ft</td>
</tr>
<tr>
<td>dpa</td>
<td>0.00 ft</td>
</tr>
<tr>
<td>dCP</td>
<td>0.0121</td>
</tr>
<tr>
<td>dLCB</td>
<td>0.0250</td>
</tr>
</tbody>
</table>

Sea kayaks typically range between 10-26 feet in length, depending on whether it is a solo or tandem vessel. Beam varies between 20-36 inches and deck height typically maxes out around 16 inches. While the beam of the sample vessel is half a foot larger than typical, the length and
height fall within the expected range. In order to produce a derived hull with obvious differences from the parent hull, sizable changes were made to the prismatic coefficient and LCB. However, the parallel midbody could not be changed for the derived hull due to variable definition issues. Both the body plan and sectional area curve above reflect the vessel as defined using the input data in Table 5.
5. Sample Results and Analysis

Using the parent and derived hull data files, the two hull forms can be compared in all aspects calculated. For completeness, the derived hull body plan and half-breadth plan are shown below; however, it is hard to see the differences in the two hull forms without reference.

![Derived hull lines plan.](image1)

Figure 11: Derived hull lines plan.

![SAC Comparison](image2)

Figure 12: Comparison of parent and derived hull sectional area curves.
Placing the sectional area curve of the derived hull over top the parent hull, the effect of the Lackenby shift becomes visible. Since the midship, forward extent of the parallel midbody, and aft extent of the parallel midbody all lie on the 8ft station, a parallel midship cannot be added as there is only one station that would have to move to two locations. This could be fixed by updating the variable definitions in the code, but currently, adding a parallel midship to a vessel that does not originally have one is impossible. Importantly, the Lackenby shift has been executed as described. The forebody areas have increased and aftbody areas decreased according to the specified forward shift of the LCB. While it is hard to analyze visually whether the overall volume has increased, thus far nothing appears amiss with the data.

Figure 13: Comparison of parent and derived hull body plans.
By overlapping the body plans of the parent and derived hulls we can analyze the changes present in the derived hull form. The top part of Figure 13 shows stations 0-10 for the parent hull (blue) and the derived hull (green) and the bottom part shows stations 11-20. The changes in volume observed in the sectional area curve are reflected in the body plan. For every station aside from midship, forward perpendicular, and aft perpendicular, the cross-sections of the derived hull stations are larger for the forebody and smaller for the aftbody compared to the parent hull.

Comparing the variables calculated for the Lackenby shift of the parent hull with the values of the derived hull can also offer valuable insight.

Table 6: Comparison of half-body variables.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Units</th>
<th>Parent Hull</th>
<th>Derived Hull</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Forebody Variables</td>
<td></td>
</tr>
<tr>
<td>iparallel</td>
<td>-</td>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>L</td>
<td>ft</td>
<td>12.00</td>
<td>12.00</td>
</tr>
<tr>
<td>CP</td>
<td></td>
<td>0.5454</td>
<td>0.6053</td>
</tr>
<tr>
<td>xLCB</td>
<td>ft</td>
<td>4.1586</td>
<td>4.2825</td>
</tr>
<tr>
<td>k</td>
<td>ft</td>
<td>5.0860</td>
<td>5.1647</td>
</tr>
<tr>
<td>R</td>
<td>ft</td>
<td>5.7766</td>
<td>5.8213</td>
</tr>
<tr>
<td>theta</td>
<td>rad.</td>
<td>-0.1258</td>
<td>-0.1296</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Aftbody Variables</td>
<td></td>
</tr>
<tr>
<td>iparallel</td>
<td>-</td>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>L</td>
<td>ft</td>
<td>8.00</td>
<td>8.00</td>
</tr>
<tr>
<td>CP</td>
<td></td>
<td>0.6914</td>
<td>0.6186</td>
</tr>
<tr>
<td>xLCB</td>
<td>ft</td>
<td>2.9631</td>
<td>2.8314</td>
</tr>
<tr>
<td>k</td>
<td>ft</td>
<td>3.5062</td>
<td>3.3953</td>
</tr>
<tr>
<td>R</td>
<td>ft</td>
<td>3.9037</td>
<td>3.8128</td>
</tr>
<tr>
<td>theta</td>
<td>rad.</td>
<td>0.1906</td>
<td>0.1789</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Other Variables</td>
<td></td>
</tr>
<tr>
<td>AM</td>
<td>ft²</td>
<td>1.3614</td>
<td>1.3614</td>
</tr>
<tr>
<td>V</td>
<td>ft³</td>
<td>16.4395</td>
<td>16.6248</td>
</tr>
<tr>
<td>CP</td>
<td></td>
<td>0.6038</td>
<td>0.6106</td>
</tr>
<tr>
<td>xLCB</td>
<td>ft</td>
<td>0.8966</td>
<td>1.3998</td>
</tr>
</tbody>
</table>
First thing of note is that the sign of every value matches expectations, particularly the entrance angle of the forebody is negative and the run angle of the aftbody is positive. This matches the orientation of the vessel in Rhino (and the stations defined in the CSV file) with the aft perpendicular laying on the origin and the vessel pointing forward into the positive x-axis. Next, \( i_{\parallel} \) for each half-body of the parent and derived hull is equal and constant. This is expected as the sample vessel has no parallel midship, so the index marking the extent of the parallel midship for all half-bodies will be equal to the index of the midship station. The half-bodies of both the parent and derived hulls are equal and add up to the LPP, which is accurate as no changes were made to add a parallel midbody. The midship area, \( A_M \), also remains identical between both vessels, which matches theory as midship is one of the stations unaffected by the Lackenby shift. Additionally, the data confirms the execution accuracy of the Lackenby shift observed visually prior. The prismatic coefficient and LCB of the forebody increased and, conversely, the same variables decreased in the aftbody. Furthermore, the overall LCB, volume, and prismatic coefficient of the vessel increased according to the input values.

However, despite the simplification that set the parent and derived half-body slopes equal, the calculated slope has changed slightly for both half-bodies. This is due to the method used to calculate the slopes. The extent of the slope was defined and calculated using the two consecutive points at the vessel extremities; however, when the station locations are shifted, the x-values used when calculating the slope of the curve are now different.
6. Conclusions

In conclusion, this project successfully demonstrated the feasibility of automating a Lackenby shift with McNaull’s expansion using Rhino’s scripting tools. Given the limitations of the testing vessel, the auxiliary scripts and the user interface worked as expected and the main script easily allows a user to create a model of a derived hull form in Rhino with minimal interaction. The current version of this code is restricted in its practical applications; however, there is ample room for improvement and expansion.

The script currently requires a CSV file input and can only perform a shift on a symmetrical hull form free of appendages. In order to further improve the ease-of-use of this script, offsetimport.py needs to be generalized to allow for point cloud or station imports from Rhino, General Hydrostastics (GHS), or other formats. This would encourage engineers to use the program as they could more easily modify a working hull model for use with the script. The cubicmatrix.py auxiliary script should be further developed to allow the bow and stern angles of the derived hull to be defined or calculated separate from the parent hull.

Additionally, appendage compatibility could be added to broaden the applicability of the script. For example, a Lackenby shift of a bulbous bow could be applied fairly easily. Everything forward of the forward perpendicular (FP) could be considered part of the bulbous bow, the cross-sectional area of the hull at the FP would be the cross section of the bulb, and the FP itself would be the “midship” of the bulb. If overall size changes were desired, the bulb could be stretched horizontally or vertically by modifying the station spacing or design draft defined by the user. The user could specify these modification ratios along with the bulb length and centroid of the parent hull. With this information, a Lackenby shift of a bulbous bow could be performed.
However, before considering additional features and capabilities, the current iteration of the code should be tested with simple hull form containing a parallel midship to prove that the Lackenby shift is being executed properly. To achieve this, definitions used to calculate the data of the derived hull form should be modified to properly execute a Lackenby shift regardless if the vessel has or is modifying a pre-existing parallel midship. With the above modifications and expansions, the script has potential to become a very comprehensive modeling tool. In concert with other Rhino tools such as Orca and Grasshopper, this script could even be used for rapid preliminary hull design testing. A number of potential hull models could be developed from a single parent hull and optimized for resistance and propulsion or a number of other design objectives.
References


Appendix A

Details:

This report, intended for readers more familiar with programming, details how the auxiliary scripts and user interface were developed and structured.

Filename:

NAME 6093 Report - Details on the Auxiliary Scripts and User Interface.pdf
Appendix B

Details:

Comma-separated values (CSV) file containing offsets for four geometric ship-like sections used within the auxiliary file secarea.py to test the functions of offsetimport.py, secarea.py, and akimaint.py.

Filename:

offsets_areatest.csv
Appendix C

Details:

Rhinoscript file that uses the auxiliary files to complete the Lackenby shift of the underwater body of a hull using station offsets provided in CSV file format. The file is executed within Rhino’s script editing window.

Filename:

main.py
Appendix D

Details:

CSV file containing offset values for a generic kayak, used to demonstrate the functionality of main.py. The offsets are defined with stations, half-breadths, and elevation values with the forward perpendicular (station 0) at the origin. Half-breadth values are defined as a fraction of the maximum half-breadth and elevation values are defined as a fraction of the design waterline.

Filename:

offsets_kayak.csv
Appendix E

Details:

Text file containing the program description, conditions, instructions usage guide, and credits for main.py and all accompanying auxiliary files.

Filename:

readme.txt
Appendix F

Details:

Python script written by Dr. Lothar Birk, University of New Orleans. Defines a function that takes a series of coordinate points split into two arrays and performs Akima interpolation on them. Also contains a test portion that demonstrates the functionality of the script.

Filename:

akimaint.py
Appendix G

Details:

Python script that defines the cubic matrix used for McNaul’s expansion of the Lackenby method.

Filename:

cubicmatrix.py
Appendix H

Details:

Python script written by Dr. Lothar Birk, University of New Orleans. Defines a function containing a simple Gaussian elimination algorithm. Also contains a small test script used to demonstrate usage of the function.

Filename:

gauss.py
Appendix I

Details:

Python script written by Dr. Lothar Birk, University of New Orleans. Defines a function to import station data from a CSV file and convert the data into coordinate points separated by station into a series of arrays.

Filename:

offsetimport.py
Appendix J

Details:

Python script containing functions for calculating sectional area, area moments, second order moment of volume, and third order moment of volume. Also contains section used to test the functionality of akimaint.py, offsetimport.py, and the functions defined within secarea.py.

Filename:

secarea.py
Appendix K

Details:

Contains the station offsets, SAC, and Lackenby shift data for the sample parent hull used introduced in Section 4.

Filename:

LackenbyShift_ParentHull.dat
Appendix L

Details:

Contains the station offsets, SAC, and Lackenby shift data for the derived hull form discussed in Section 5, found from the sample vessel introduced in Section 4.

Filename:

LackenbyShift_DerivedHull.dat
Vita

The author was born in Seattle, Washington. She obtained her Bachelor’s degree in naval architecture and marine engineering from the University of New Orleans in 2021. She continued to pursue a Master’s degree in naval architecture and marine engineering from the University of New Orleans, working with Dr. Lothar Birk on the automation of hull design using programming.